

MI JAN 07

1) $R_f \uparrow = 0 \Rightarrow \frac{1}{2}P = 24 \Rightarrow P = 48N$
 $R_f = 0 \quad 0.866P = Q \Rightarrow Q = 41.6N$

2) $\sum \tau = 0 \Rightarrow 80 \times x = 120 \times 0.5$
 $80x = 60$
 $x = \frac{60}{80} = 0.75m$

b) $\sum \tau = 0 \Rightarrow 120 \times 1.25 = W \times 2.5$
 $1.25W = 30$
 $W = 24N$
 $R_f \uparrow = 0 \Rightarrow 120 + W = NR_b$
 $NR_b = 144N$

d) particle \rightarrow no physical size, so weight acts exactly at the end of the plank.

3) $acc = \frac{\text{change in vel}}{\text{time}} = \frac{12i - 6j}{4} = 3i - 1.5j \text{ ms}^{-2}$

b) $F = Ma \Rightarrow R_f = 2(3i - 1.5j) = 6i - 3j \quad R_f = \sqrt{6^2 + 3^2} = 6.7N$

c) $Vel = \text{original vel} + t(acc) \Rightarrow V = (3i + 2j) + 6(3i - 1.5j)$
 $V = 21i - 7j \text{ ms}^{-1}$

4) $\text{total mom before} = 0.3 \times u + 0 = 0.3u$
 $\text{total mom after} = 0.3 \times -2 + 0.6 \times 5 = -0.6 + 3$
 $\Rightarrow 0.3u = -0.6 + 3 = 2.4 \Rightarrow u = 8 \text{ ms}^{-1}$

b) $\text{Mom } Q \text{ before} = 0 \quad \text{Mom } Q \text{ after} = 3Ns \Rightarrow \text{Impulse} = 3i$

c) $\text{Impulse to bring } Q \text{ to rest} = 3Ns$
 $\text{Impulse} = \text{force} \times \text{time} \Rightarrow 3 = R \times 1.5 \Rightarrow R = 2N$

5) $u \uparrow = 21 \quad v^2 = u^2 + 2as \Rightarrow 0 = 21^2 - 19.6s$
 $a \uparrow = -9.8 \quad s = 22.5m$
 $v \uparrow = 0 \text{ (at greatest height)} \quad \text{total height} = 22.5 + 1.5 = ?$

b) $u \uparrow = 21 \quad a \uparrow = -9.8 \quad s = -1.5m \quad v = u + at$
 $v = 21 + (-9.8) \times (-1.5)$
 $v^2 = u^2 + 2as \Rightarrow v^2 = 21^2 + 2(-9.8)(-1.5)$
 $\Rightarrow v^2 = 470.4 \Rightarrow v = 21.7 \text{ ms}^{-1} \downarrow$

c) $u \uparrow = 21 \quad a \uparrow = -9.8 \quad v \uparrow = -21.7$

$v = u + at \Rightarrow -21.7 = 21 - 9.8t \quad t = \frac{-42.7}{-9.8} = 4.36 \text{ sec}$

6) $\text{Constant speed} \Rightarrow R_f = 0$
 $R_f \uparrow = 0 \Rightarrow NR = 294 - 0.342P$
 $R_f = 0 \Rightarrow f_{max} = 0.94P$
 $f_{max} = \mu NR \Rightarrow 0.94P = 0.4(294 - 0.342P)$
 $\Rightarrow 0.94P = 117.6 - 0.137P$
 $1.08P = 117.6 \Rightarrow P = 109.2N$

b) $R_f \uparrow = 0 \quad NR = 30g - 150 \sin 20$
 $NR = 242.7N$
 $R_f = ma \Rightarrow 140.95 - f_{max} = 30a$
 $\Rightarrow 43.9 = 30a \Rightarrow a = 1.46m/s^2$
 $f_{max} = 0.4(242.7) = 97.1$

7) $R_f = ma \Rightarrow T - 1.5g = 3a$
 $R_f \downarrow = ma \Rightarrow 2g - T = 2a$
 $0.5g = 5a$
 $\Rightarrow a = 0.1g$
 $a = 0.98 \text{ ms}^{-2}$
 $T = 3a + 1.5g = 17.64N$

a) μ latex
 d) Inextensible \Rightarrow same acceleration for P and Q.

c) $u \downarrow = 0 \quad s = 0.8 \quad a \downarrow = 0.98$
 $v^2 = u^2 + 2as \Rightarrow v^2 = 2(0.98)(0.8) \Rightarrow v = 1.25 \text{ ms}^{-1}$

f) $T = 0$
 $R_f = ma \Rightarrow -1.5g = 3a \Rightarrow a = -0.5g$
 $u \uparrow = 1.25 \quad v \uparrow = 0$
 $v = u + at \Rightarrow 0 = 1.25 - 4.9t$
 $t = 0.255 \text{ sec.}$

0.255 sec for P to reach greatest height of slope
 \Rightarrow 0.51 sec to return to the point it was at when Q hit the ground; 0.51 sec for the string to become taut again.